# INTORDUCTION TO ALGORITHMS – EC351 ASSIGNMENT – 3

1. **Find out Time complexity for the arrays using Quick Sorting and Merge SortingAlgorithms**

**Sol :**

**Merge Sorting Algorithms :**

**CODE :**

from datetime import datetime start\_time = datetime.now()

def merge\_sort(arr, begin, end):

if end - begin > 1:

middle = (begin + end)//2 merge\_sort(arr, begin, middle) merge\_sort(arr, middle, end) merge\_list(arr, begin, middle, end)

def merge\_list(arr, begin, middle, end): left = arr[begin:middle]

right = arr[middle:end] k = begin

i =0

j =0

while (begin + i < middle and middle + j < end): if (left[i] <= right[j]):

arr[k] = left[i] i = i + 1

else:

arr[k] = right[j] j = j + 1

k = k + 1

if begin + i < middle: while k < end:

arr[k] = left[i] i = i + 1

k = k + 1

else:

while k < end: arr[k] = right[j] j = j + 1

k = k + 1

arr = input('Enter the list of numbers: ').split() arr = [float(x) for x in arr]

merge\_sort(arr, 0, len(arr)) print('Sorted list: ', end='') print(arr)

end\_time = datetime.now()

print('Duration : {}'.format(end\_time - start\_time))

## ALGORITHM :

MergeSort(arr[], l, r) If r > l

**STEP 1**. Find the middle point to divide the array into two halves: middle m = (l+r)/2

**STEP 2**. Call mergeSort for first half: Call mergeSort(arr, l, m)

**STEP 3**. Call mergeSort for second half: Call mergeSort(arr, m+1, r)

**STEP 4.** Merge the two halves sorted in step 2 and 3: Call merge(arr, l, m, r)

## INPUT ARRAY :

**1. A [2.5, 4.5, 3.0, 1.2, 6.5, 8.9, 7.4, 6.3] OUTPUT :**

**Enter the list of numbers:** 2.5 4.5 3.0 1.2 6.5 8.9 7.4 6.3

**Sorted list:** [1.2, 2.5, 3.0, 4.5, 6.3, 6.5, 7.4, 8.9]

## 2. B [5 3 6 3 4 5 4 6 4 ]

**Enter the list of numbers:** B [5 3 6 3 4 5 4 6 4 ]

**Sorted list:** [3.0, 3.0, 4.0, 4.0, 4.0, 5.0, 5.0, 6.0, 6.0]

# Time complexity For Merge Sorting Algorithms:

Merge Sort is a recursive algorithm and time complexity can be expressed as following recurrence relation.

## T(n) = 2T(n/2) + O(n)

Time complexity of Merge Sort is **O(nlogn)** in all 3 cases (worst, average and best) as merge sort always divides the array into two halves and take linear time to merge two halves.

# Quick Sorting Algorithm: CODE :

from datetime import datetime start\_time = datetime.now() def quicksort(arr, begin, end):

if end - begin > 1:

p = partition(arr, begin, end)

quicksort(arr, begin, p) quicksort(arr, p + 1, end)

def partition(arr, begin, end): pivot = arr[begin]

i = begin + 1 j = end - 1

while True:

while (i <= j and arr[i] <= pivot): i = i + 1

while (i <= j and arr[j] >= pivot): j = j - 1

if i <= j:

arr[i], arr[j] = arr[j], arr[i] else:

arr[begin], arr[j] = arr[j], arr[begin] return j

arr = input('Enter the list of numbers to be Sorted: ').split() arr = [float(x) for x in arr]

quicksort(arr, 0, len(arr)) print('Sorted list: ', end='') print(arr)

end\_time = datetime.now()

print('Duration : {}'.format(end\_time - start\_time))

## ALGORITHM :

**Quick Sort Pivot Algorithm :**

**Step 1** − Choose the highest index value has pivot

**Step 2** − Take two variables to point left and right of the list excluding pivot

**Step 3** − left points to the low index

**Step 4** − right points to the high

**Step 5** − while value at left is less than pivot move right

**Step 6** − while value at right is greater than pivot move left

**Step 7** − if both step 5 and step 6 does not match swap left and right

**Step 8** − if left ≥ right, the point where they met is new pivot

## QUICK SORT ALGORITHM :

**Step 1** − Make the right-most index value pivot **Step 2** − partition the array using pivot value **Step 3** − quicksort left partition recursively **Step 4** − quicksort right partition recursively

## INPUT ARRAY :

**1. A [2.5, 4.5, 3.0, 1.2, 6.5, 8.9, 7.4, 6.3] OUTPUT :**

**Enter the list of numbers to be sorted:** 2.5 4.5 3.0 1.2 6.5 8.9 7.4 6.3

**Sorted list:** [1.2, 2.5, 3.0, 4.5, 6.3, 6.5, 7.4, 8.9]

## 2. B [5 3 6 3 4 5 4 6 4 ]

**Enter the list of numbers to be sorted:** B [5 3 6 3 4 5 4 6 4 ]

**Sorted list:** [3.0, 3.0, 4.0, 4.0, 4.0, 5.0, 5.0, 6.0, 6.0]

## TIME COMPLEXITY OF QUICK SORT ALGORITHM:

**Best case :**

To find the location of an element that splits the array into two parts, O(n) operations are required.

* This is because every element in the array is compared to thepartitioning element.
* After the division, each section is examinedseparately.
* If the array is split approximately in half (which is not usually), then therewill be lognsplits.
* Therefore, total comparisons required are f(n) = n x logn =O(nlogn).
* Order of Quick Sort in best case = O(nlogn).

# Worst Case :

Quick Sort is sensitive to the order of input data.

* It gives the worst performance when elements are already in theascending order.
* It then divides the array into sections of 1 and (n-1) elements in eachcall.
* Then, there are (n-1) divisions inall.
* Therefore, here total comparisons required are f(n) = n x (n-1) =O(n2).
* Order of Quick Sort in worst case =O(n2)

# Find out Arrays Sorting program execution timeusing python orC++.

**Sol: Execution time using Python : - Quick sort algorithm execution time:**

**1.**

Enter the list of numbers to be Sorted: 2.5 4.5 3.0 1.2 6.5 8.9 7.4 6.3

Sorted list: [1.2, 2.5, 3.0, 4.5, 6.3, 6.5, 7.4, 8.9]

**Duration : 0:00:23.270743**

**2.**

Enter the list of numbers to be Sorted: 5 3 6 3 4 5 4 6 4

Sorted list: [3.0, 3.0, 4.0, 4.0, 4.0, 5.0, 5.0, 6.0, 6.0]

**Duration : 0:00:37.650884**

**Merge sort algorithm execution time :1.**

Enter the list of numbers: 2.5 4.5 3.0 1.2 6.5 8.9 7.4 6.3

Sorted list: [1.2, 2.5, 3.0, 4.5, 6.3, 6.5, 7.4, 8.9]

**Duration : 0:00:32.074479**

**2.**

Enter the list of numbers: 5 3 6 3 4 5 4 6 4

Sorted list: [3.0, 3.0, 4.0, 4.0, 4.0, 5.0, 5.0, 6.0, 6.0]

**Duration : 0:00:26.142812**

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